

# **GEOG 4185/5185**

## **STATISTICAL RESEARCH METHODS IN GEOGRAPHY**



## **Review – Section #1\***

### **Covering**

- **Week 1:** Motivation & Fundamentals
- **Week 2:** Probability, Distributions, Z-Scores
- **Week 3:** Normal and Poisson Probabilities, Statistical Testing Basics
- **Week 4:** Tails in Testing and Sampling Issues

\* This content connects with labs done in weeks 1-4 and quiz #1 (week 4).

## **Week I: Motivation & Fundamentals**

### **Statistics: Why?**

#### **Definition and goal of statistics**

#### **Four distinctive uses of statistics**

1. Descriptive
2. Inferential
3. Significance
4. Prediction

#### **More terminology**

- Element
- Sample
- Population
- Variable

#### **General Sampling Issues**

- Randomness
- Sample Size

### **Specific Problems in Sampling**

- Unknown population
- Known population that can't be sampled
- Population too small for sampling
- Sampling bias

### **Use of Statistics in Context of Samples**

- Inferential Applications
- Descriptive Applications

### **Discussion on Honest Statistics**

### **Scales of Measurement**

- Nominal
- Ordinal
- Interval
- Ratio

### **Conversion Between Scales**

### **Geographical Data Cube**

## **Week 2: Probability, Distributions, Z-Scores**

### **Probability as a Central Idea for the Course**

### **Side Discussion: Math Notation (View Supplemental Video)**

### **Understanding Probability**

Two key kinds of probabilities

1. Theoretical Probabilities
2. Empirical Probabilities

### **Communicating Probabilities**

### **Combining Probabilities**

### **The Frequency Distribution Idea**

### **Theoretical versus Empirical Distributions**

## **Two Common Theoretical Frequency Distributions**

1. Normal Distribution
2. Poisson Distribution

## **General Uses for Theoretical Distributions**

- Parametric versus Non-Parametric Methods

## **Z-Scores**

- How to calculate
- What they mean

# **Week 3: Normal & Poisson Probabilities, and Statistical Testing Basics**

## **The Normal Distribution**

### **Characteristics that Make it Important**

**Mean = Median = Mode**

**Area under the Normal Curve = 1.0 (100%)**

### **Fitting the Normal Curve to an Empirical Dataset**

#### **Sample Probability Distribution**

- Steps to fit a normal curve to an empirical probability distribution
- Table that captures the overall process

### **Using and Interpreting a Normal Probability Table**

## **The Poisson Distribution**

### **Reminder of Interpretation and Meaning**

**Example #1: Grid on a Map, Do Counts**

**Example #2: Hailstorm Observations**

## **Significance Testing**

### **Significance Testing and Statistical Testing**

#### **Key Significance Testing Subtopics**

1. Hypotheses
  2. Assumptions
  3. Test Statistics
  4. Sampling Distributions/Critical Values
  5. Degrees of Freedom
- What this looks like in an Example

## **Week 4: Tails in Testing, Types of Errors, and Sampling Issues**

### **One and Two-Tailed Tests**

#### **Difference Between One and Two-Tailed Tests**

- Meaning

#### **Two-Tailed Test Case**

#### **One-Tailed Test Case**

### **Samples and Sampling**

#### **Two Major Types of Sampling Methods**

1. Random
2. Systematic

**Also, can take a spatial or aspatial approach to each**

#### **Random Sampling**

- Random Sampling as Statistically Most Justifiable
- Issue of Replacement
- Reasons for Not Preferring a Pure Random Approach

#### **Systematic Sampling**

- Employing brings issues

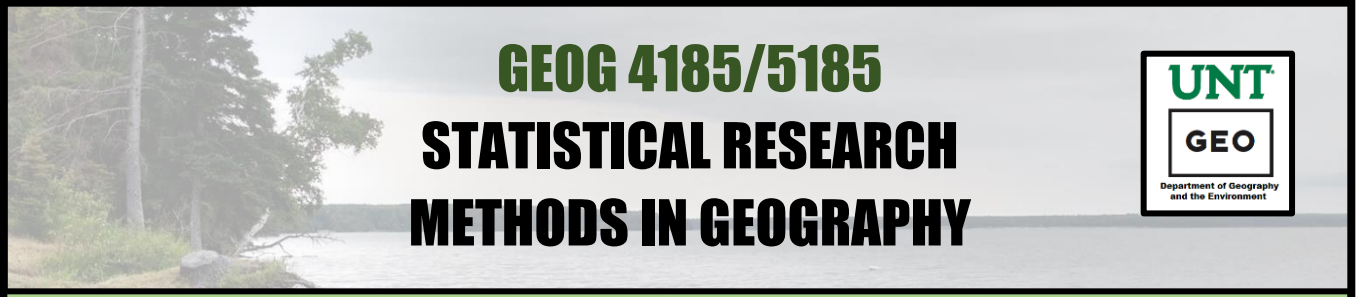
### **Stratified Sampling**

- Combination of Random and Systematic

### **Spatial Sampling**

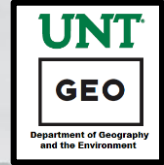
- Simple Random
- Simple Systematic
- Stratified Random
- Cluster Sampling

### **Overall Thoughts on Sampling**



# **GEOG 4185/5185**

## **STATISTICAL RESEARCH METHODS IN GEOGRAPHY**



## **Review – Section #2**

### **Covering**

- **Week 5:** Data Description & Transformations
- **Week 6:** Estimates from Samples, Sample Size Determination
- **Week 7:** Comparative Statistics – Mann-Whitney U Test, t-Test
- **Week 8:** Chi-Square Test (1 Sample, 2 Sample, 3 or More Sample)

\* This content connects with labs done in weeks 5-8 and quiz #2 (week 8).

## **Week 5: Data Description and Transforming Data Distributions**

### **Description**

#### **Central Tendency**

#### **Dispersion**

#### **Characteristics of Frequency Distributions**

- Skewness
- Kurtosis

#### **Transformations**

#### **Why Transformations?**

#### **Sample Application: Eliminating Skewness**

# **Week 6: Estimates from Samples, Sample Size, and a Start on Comparative Methods**

## **Samples and Sample Size**

### **Estimates from Samples**

1. Estimating the Mean
2. Estimating the Standard Deviation
3. Estimates from Small Samples
4. Estimating Proportions
5. Sample Size

## **Overview of Comparative Tests**

### **The Valley of Statistical Tests**

- A. K-S Test
- B. Runs Test for Randomness
- C. Mann-Whitney U Test
- D. Student's  $t$  Test (One or Two Tailed)
- E. Chi-Square Test
- F. Kruskal-Wallis H Test
- G. Analysis of Variance (ANOVA)

### **Six Steps of a Formal Statistical Test (Video Supplement)**

1. Formulate Hypotheses
2. Select a Test Statistic
3. Select a Significance Level
4. Determine the Critical Value
5. Calculate the Test Statistic
6. Make a Decision

## **Example of Application of a Formal Statistical Test**

### **Kolmogorov-Smirnov Test of Goodness of Fit**

- Basic Overview
- Example: Comparing an Observed Distribution with a Theoretical Distribution (Rainfall)
- Example: Comparing an Observed Distribution with Model Predictions (Tributaries on a Stream)

# **Week 7: Comparative Statistical Methods, Part I – Mann-Whitney U Test, Student's t Test**

## **Mann-Whitney U Test**

Basic Overview

Three Different Use Cases for  
Example: Comparing Two Soil Samples

Properties of the U Sampling Distribution

## **Student's t Test**

Basic Overview

Assumptions

Testing Options

One-Sample, Paired-Samples, Independent Sample

A. One-Sample Case

Example: Calorie Intake Study

B. Paired-Samples Case

Example

C. Independent Sample Case

# **Week 8: Comparative Statistical Methods – Part II, Chi Square Test**

## **Chi Square Test**

Basic Overview

One Sample Case

One Sample Example: Farm Types

Two Sample Case

Subcase 1: compare two situations with same expectation

Example: Glacial Features

Example: Political Affiliations

Subcase 2: compare two situations with different expectations

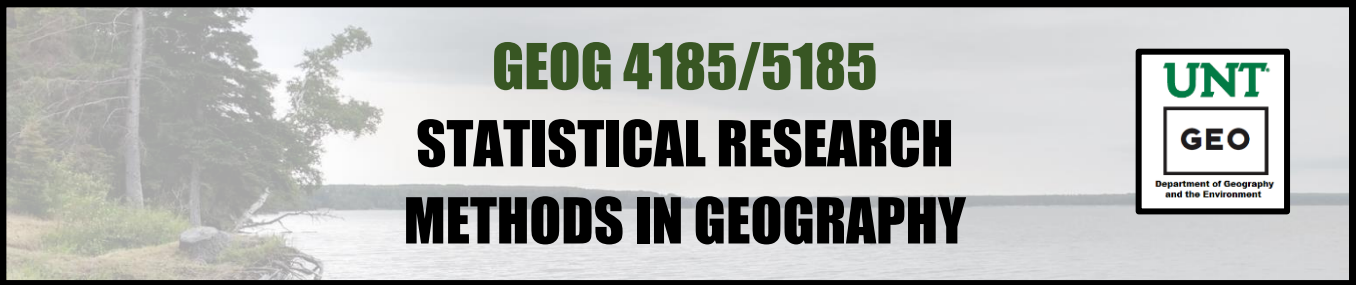
Example: Car Purchases by Metro Area

Three or More Sample

Example: Land Use/Land Cover

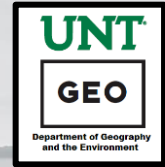
Overall Summary of Comparative Statistical Tests





# **GEOG 4185/5185**

## **STATISTICAL RESEARCH METHODS IN GEOGRAPHY**



## **Review – Section #3\***

### **Covering**

- **Week 9:** ANOVA, Kruskal-Wallis H Test
- **Week 10:** Relationships – Correlation
- **Week 11:** Trends – Linear Regression
- **Week 12:** Trends – Multiple Regression
- **Week 13:** Spatial Statistics – Point and Areal Patterns
- **Week 14:** Spatial Statistics – Trend Surface Analysis

\* There is no quiz that covers this material, but the content in this section connects with the final labs in this course.

## **Week 9: Comparative Statistical Methods – Part III, ANOVA (One-Way, Two-Way, Three-Way), Kruskal-Wallis H Test**

### **ANOVA**

Basic Overview

Use: for 3 or more Samples (interval/ratio data)

Variance Decomposition Concept

Example: July High Temperatures in Texas

ANOVA and Correlation Analysis

Applications for a Significant ANOVA Result

### **Kruskal-Wallis H Test**

Basic Overview

Use: for 3 or more Samples (ordinal data)

### **Errors in Statistical Testing**

Type I Error

Type II Error

## Week 10: Correlation

### The idea of relationship as we have already studied it in this course

- Parallels with the overall concept
- Ways in which relationship as discussed here is less than satisfactory

### Contribution of correlation

- How strong is the relationship?
- We need a measure of relationship strength

### Correlation in a bivariate context

- Look at a spectrum of cases
  - o Perfect, direct ( $r = +1.0$ )
  - o Imperfect, direct ( $r = +0.7$ )
  - o No relationship ( $r = 0.0$ )
  - o Imperfect, indirect ( $r = -0.7$ )
  - o Perfect, indirect ( $r = -1.0$ )

### Correlation versus Causation

- Not equivalent

## Week 11: Introduction to Regression

### Trends as a general concept

Idea of curve fitting

### Simple Linear Regression

Goodness of fit possibilities (from data points to best fit line)

- Minimize sum of distances, distances measured at a right angle to fitted line)
- Minimize total area of triangles created between data and line
- Same as A, but distance measured in vertical direction
- Same as C, but distance is squared

### Regression Subtopics

Calculation  
Analysis of residuals  
Outliers  
Assumptions for simple linear regression  
Confidence limits

## **Week 12: Multiple Correlation and Regression**

### **Introduction to Multivariate Case**

- Comparison with topics of past two weeks
- Idea of surface fitting instead of best-fit line
- Visualization of multivariate datasets to set up for multiple correlation and regression

### **Multiple Correlation**

- Partial Correlation Coefficients
- Multiple Correlation Coefficient

### **Multiple Regression**

- Partial Regression Coefficients
- Beta Coefficients
- Multicollinearity: The Problem
- Approaches to Multicollinearity
- Dummy Variables
- Data Issues
- Multiple Regression in a Geographic Context

## **Week 13: Spatial Statistics**

### **Cases Addressed**

- Point
- Area

### **Point Distributions**

- Summary Statistics
  - Examples
- Nearest Neighbor Concept
  - Examples
- Nearest Neighbor Analysis
  - Calculation of Nearest Neighbor Index
  - Question of Significance
  - Geary's C

### **Areal Patterns**

- Introduction
  - Examples
- Dichotomous Case
- Continuous Case

## **Dichotomous Case: Join Count**

Issues  
Calculations

## **Continuous Case: Moran's I**

Issues  
Contiguity Matrix  
Example: Incomes by State

## **Brief Discussions: Further Methods**

Hot Spot Analysis (Getis-Ord  $G_i^*$ )  
Local Moran's I

# **Week 14: Spatial Pattern – Smoothing and Trend Surface**

## **Smoothing and Trend Surface**

Basic Ideas

## **Spatial Smoothing**

Definition of Application  
Example: Cancer in Belarus  
Example: Oceanic Air Pressure Map  
Example: Tijuana River Watershed  
Basic Methods  
1. Interpolation  
2. Running Mean  
a. One Dimension  
b. Two Dimensional Filter Mapping  
c. Problems

## **Trend Surface Analysis**

Basic Concepts  
Orders of Equations  
Planar  
Quadratic  
Residual Analysis  
Example: Settlement Development in Pennsylvania  
Example: Iowa Weather Stations

## **Connections to our Spatial Analysis Lab**